Terahertz-wave emission from Bi2212 intrinsic Josephson junctions: a review on recent progress

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Abstract. Emission of terahertz (THz) electromagnetic (EM) waves from a high critical temperature (T_c) superconductor intrinsic Josephson junction (IJJ) is a new and promising candidate for practical applications of superconducting devices. From the engineering viewpoint, the IJJ THz source is competitive against the present semiconducting THz sources such as quantum cascade lasers and resonance tunnelling diode oscillators because of its broad tunable frequency range and ease of the fabrication process for the device. The emitted EM waves are considered to be coherent because the emission is yielded by synchronisation of thousand stacked IJJs consisting of the mesa device. This synchronisation is peculiar: the resonant frequency of each IJJ is distributed because the cross section of the mesa device is trapezoidal in shape. One of the key features of the synchronisation mechanism is the temperature inhomogeneity of the emitting device. In this topical review, we describe the recent progress in studies of IJJ THz sources with particular emphasis on the relevance of the temperature inhomogeneity to the synchronisation and the emission intensity. This review is of specific interest because the IJJ THz source shows the rich variety of functions due to self-heating which has always been a detrimental feature in the present superconducting devices. Moreover, the thermal managements used for IJJ THz sources will be common with those of other semiconducting devices such as quantum cascade lasers. In addition, this review is to invite the readers into related research through the detailed descriptions of experimental procedures.

Keywords: High- T_c cuprate, intrinsic Josephson junction, Terahertz electromagnetic wave, synchronization effect, self heating Submitted to: Supercond. Sci. Technol.

Contents

1 Introduction

2	Comparison of IJJ THz source with other THz sources			
3	Electromagnetic wave excitations in IJJs	5		
4	Experimental methods and emission properties4.1Device preparation and measurement setups4.2AC Josephson relation and cavity effect4.3Emission intensity4.4Suitable materials	8 8 11 15 17		
5	Thermal management of IJJ THz sources5.15.2Heat manipulation	19 20 22		
6	6 Examples of applications of terahertz EM wave sources			
7	Summary	26		

2

1. Introduction

The discovery of the Josephson effect [1] in superconducting tunnel junctions illuminates the macroscopic quantum nature of superconductivity, in which the tunneling supercurrent is given by the sine of the phase difference of the macroscopic wave functions. The DC voltage across superconducting electrodes of a Josephson junction induces temporal development of the gauge-invariant phase difference between the electrodes. This was soon supported by the observation of the Fiske resonance in the presence of an external magnetic field [2]. The induced electromagnetic (EM) wave inside the tunnel barrier is established as the phase collective mode and is referred to as a Josephson plasma oscillation [3]; its frequency is given by the maximum Josephson current and the capacitance of the junction in the long-wavelength limit. The use of the Josephson plasma oscillation as an EM wave source has been a long-term quest for researchers in the field of superconductivity.

The first direct detection of EM wave radiation from single Josephson junctions was reported by Yanson et al [4] and Langenberg et al. [5] in 1965. The radiations were detected when the junction was biased on one of the Fiske steps, and the radiation powers were on the order of 1 pW at about 10 GHz. Higher radiation powers were obtained from one- and two-dimensional arrays of synchronized Josephson junctions; for example, an array of thousands of Josephson junctions delivered a power of 160 μ W at a frequency of 240 GHz [6].

The demonstration of the intrinsic Josephson effect in Bi₂Sr₂CaCu₂O_{8+ δ} (Bi2212) and other layered superconductors [7] and subsequent findings of various phenomena in these intrinsic Josephson junctions (IJJs) [8] strongly stimulated the research toward superconducting EM wave sources in the terahertz (THz) frequency region. Since the superconducting order parameter is strongly modulated along the *c*-axis with a period of a (half) unit cell of the crystal structure of the superconductor, a single crystal can be considered as a stack of Josephson junctions consisting of superconducting electrodes and barrier layers with thicknesses of 0.3 and 1.2 nm, respectively for Bi2212. This is in sharp contrast to a conventional Josephson junction, in which thick electrodes are connected through an oxide barrier with a thickness of less than ~ 1 nm (several atomic layers). There are two main reasons why a stack of IJJs is suitable for use as a THz source. (1) A huge number of Josephson junctions are accumulated in a single crystal of Bi2212. For instance, a crystal with a thickness of 0.1 mm contains 70,000 junctions, which are strongly connected in series by the inductive [9] and capacitive [10, 11] couplings. The emission intensity is expected to be proportional to the square of the number of synchronous oscillators. (2) The large superconducting gap Δ , which is greater than tens of meV in Bi2212 [12], protects the phase coherence from high-frequency damping. This results in the excitation of a highly coherent EM wave in the THz region. The theoretical upper limit of the excited EM wave is approximately 10 THz for $\Delta \approx 50$ meV. This is in sharp contrast to Josephson junctions made of Nb with critical temperature T_c of 9 K, where the superconducting gap corresponds to 0.7 THz according to the Bardeen-Cooper-Shrieffer theory, $\Delta = 3.53k_BT_c$.

The first milestone for the EM wave radiation from IJJs was elucidation of the Josephson plasma resonance [13, 14, 15, 16, 17, 18]. Intensive studies of the Josephson plasma resonance revealed the damping mechanism of Josephson tunnelling [19] in cuprates and novel phase transitions in the vortex phase diagram [20, 21, 22, 23]. The second milestone was the observation of various geometric effects in tiny crystals under magnetic fields parallel to the *ab*-plane. The oscillation of the *c*-axis resistivity indicates the formation of a triangular Josephson vortex (JV) lattice [24]. The Fiske steps elucidate that the DC voltage bias excites a Josephson plasma wave that propagates along a reciprocal vector of a JV lattice [25, 26]. The results suggest that in-plane magnetic fields may facilitate synchronisation among the stacked IJJs in certain cases [27, 28]. The third and most impressive milestone is the detection of sub-THz EM waves radiated from an IJJ mesa structure into the space outside the cryostat in the absence of an external magnetic field, which was achieved in 2007 [29] and is the main concern of this article. Subsequent research revealed a quite peculiar feature of the IJJ THz source among superconducting devices: an inhomogeneous temperature distribution. In fact, even a local temperature rise, which is always detrimental to the superconducting properties, is an essential ingredient for IJJ THz sources.

This review focuses on the relevance of the temperature distribution for high- T_c IJJ THz sources, and is organised as follows. Section 2 describes the IJJ THz source by comparing it with other candidates for THz sources. Section 3 gives a brief history of Josephson plasma excitations and the emission of EM waves in IJJs. Section 4 reviews the experimental details of IJJ THz sources. Section 5 describes the state of the art technology for thermal management of IJJ THz sources. The challenges and perspectives for their practical application are discussed in Sec. 6. Finally, this article is summarised in Sec. 7.

2. Comparison of IJJ THz source with other THz sources

In this section, the properties of an IJJ THz source are briefly reviewed to illustrate the comparison with other continuous-wave (CW) sources such as a quantum cascade laser (QCL), and a resonance tunnel diode (RTD) oscillator. Figure 1 (a) and (b) show the operating temperature and emission power of three types of THz sources (IJJ THz source [30, 31, 32, 33, 34], THz-QCL [35, 36, 37, 38, 39, 40, 41], and RTD oscillator [42, 43, 44, 45]) as functions of the frequency filling up the THz gap [46].

The most frequently investigated source is the QCL, which consists of a repeated stack of GaAs-based multiple quantum well heterostructures fabricated by molecular



Figure 1. (a) Operation regions in temperature versus frequency of IJJ THz sources, in which the device structures are optimized for thermal management. A hatched area edged by solid lines represents the emission frequency region of one device. Three areas shown by red, green, and blue are obtained from the sandwich structure of a rectangular stack[33], the sandwich structure of a cricular stack[34], and the gold-Bi2212-gold structure[32], respectively. Performances of CW QCLs, pulsed QCLs, and RTD oscillators are indicated by solid squares, open squares, diamonds, respectively. Data indicated by "with **B**" are taken from pulsed QCLs under magnetic field. (b) Maximum emission powers of IJJ THz sources (spheres), CW QCLs (squares), and RTD oscillators (diamonds). Colors of symbols represent measurement temperature for IJJ THz sources and CW QCLs.

beam epitaxy [47, 48]. The emission frequency f_e is determined by the optical transition between subbands formed in quantum well systems. Since the emission is based on population inversion between the two levels, the operating temperature is roughly limited by the thermal fluctuation; *i.e.*, $T < hf_e/k_B$, where h and k_B are the Planck constant and Boltzmann constant, respectively [49, 50]. In pulsed bias operation with a repetition frequency of ~ 100 kHz and a duty cycle of less than 5 %, the operating temperature significantly exceeds the upper limit up to $T > 2hf/k_B$ [36, 41, 50] as shown in Fig. 1 (a) by open squares. To extend the frequency downward to the sub-THz region, population inversion between two Landau levels of a two dimensional (2D) electron gas under a high magnetic field (> 5 T) perpendicular to the layers is used [51, 38, 39]. Magnetically assisted QCLs are also operated with pulsed biases.

An RTD oscillator based on semiconductor quantum wells has been developed from operation in a lower frequency region [52]. The emission occurs in a negative differential resistance region of the device. The emission frequency is determined by the capacitance of the device and the length of the antenna and can be tuned within a few percent by varying V. The highest operating frequency is 1.4 THz at a power of 1 μ W for devices with submicron mesas and antennas [45]. The emission power P decreases dramatically with increasing frequency because of the decrease in the bias current.

In comparison with these THz sources, the IJJ THz source has following advantages:

- Since the superconducting gap protects the phase coherence from thermal damping, the emission frequency f_e is not limited by temperature.
- The emission frequency can be easily tuned by varying the operating bath temperatures T_b and bias voltage V: the state-of-the-art maximum tuning range is 0.3 2.4 THz [34]. This is in sharp contrast to the other two devices, the emission frequencies are determined by the device fabrication.
- Since the device function is based on the intrinsic crystal structure, highly sophisticated nanotechnologies such as molecular beam epitaxy and e-beam lithography are not required for their production. Thus, the preparation for starting research and development of IJJ THz sources is less demanding than those for studying other sources.

IJJ THz sources often exhibit the strongest emission around 0.5 THz with a T_b of 30-50 K, where QCLs do not operate in the CW mode because the population inversion collapses. The emission power is more than one-order higher than that of the RTD oscillator between 0.3 and 1 THz. The emission frequency of IJJ sources decreases with increasing T_b . Thus, the lowest emission frequency is obtained at the highest temperature, at which the active region of the device is considered to be just below the superconducting transition temperature T_c . With decreasing T_b , the emission frequency increases, and the highest P is obtained at frequencies corresponding to the geometrical resonances. These phenomena are described in detail in the following sections.

3. Electromagnetic wave excitations in IJJs

This section briefly describes the historical background from the observation of the Josephson plasma resonance to demonstration of the THz emission in IJJs.

The experimental and theoretical developments regarding EM response of IJJs are surveyed, and the distinguishing features of the discovery in 2007 are noted.

The emission of an EM wave from IJJs under a DC bias voltage is based on excitation of synchronised Josephson plasma oscillations in stacked IJJs. The Josephson plasma resonance has been investigated as a probe for Josephson and quasiparticle tunnelling and phase coherence along the c-axis. More detailed theoretical treatments of Josephson plasma excitation in contrast to the conventional Josephson junctions are described in Ref. [53].

The Josephson plasma resonance in layered superconductors was discovered by Tamasaku et al in $(La,Sr)_2CuO_4$, [13] and subsequently found by Tsui et al in Bi2212 [14]. Consider a spatially dependent and time-dependent gauge-invariant phase difference $\phi_{l,l+1}(x,t)$ between the l and l + 1-th CuO₂ double layers of Bi2212 IJJs. Two phase collective (Josephson plasma) excitations are possible: the transverse mode uniform along the *c*-axis (*z*-direction) and the longitudinal mode uniform over the *ab*-plane (*xy*-direction) as shown in Figs. 2 (a) and (b), respectively. Note that the Josephson current between the *l*-th and *l*+1-th superconducting layers flows according to the DC Josephson formula as:

$$J_{l,l+1}(x,t) = J_c \sin \phi_{l,l+1}(x,t),$$
(1)

where J_c is the maximum Josephson current density between two superconducting layers and $\phi_{l,l+1}$ is the gauge invariant phase difference between the *l*-th and *l* + 1-th layers. The dispersion relation of the transverse Josephson plasma wave propagating along the *x*-axis with a wave number of k_x is given by

$$\omega(k_x) = \omega_p \sqrt{1 + k_x^2 \lambda_c^2},\tag{2}$$

where $\omega_p = c_0/\sqrt{\epsilon}\lambda_c = \sqrt{2edJ_c/\hbar\epsilon}$ and $\lambda_c \sim 100\mu$ m are the Josephson plasma frequency and *c*-axis penetration depth, respectively. Here, c_0 , d, and ϵ denote the speed of light in vacuum, the separation between superconducting layers, and the highfrequency dielectric constant, respectively. The dispersion relation of the longitudinal Josephson plasma wave is given by

$$\omega(k_z) = \omega_p \sqrt{1 + k_z^2 \mu^2},\tag{3}$$

where $\mu \sim 1$ nm is the charge screening length [53]. In Bi2212, $\omega_p/2\pi$ is known to be ~ 100 GHz; thus, $\omega(k_x)$ can be in the THz frequency range when k_x is on the order of 0.1 μ m⁻¹ (a wavelength of several tens μ m) for the transverse mode.

The wavelength of an excited Josephson plasma wave inside an IJJ stack is roughly determined by its geometry, as will be discussed in Sec. 4.2. The non-linear Josephson plasma oscillation with a frequency f is induced when a bias voltage v is applied across an IJJ as

$$f = 2ev/\hbar,\tag{4}$$

where e represent elementary charge (AC Josephson relation). Strong emission occurs when the Josephson plasma waves in hundreds of stacked IJJs are synchronous. The synchronisation mechanism of IJJs is of broad interest in physics and applied mathematics because the stacked IJJs have distributed resonance frequencies due to the trapezoidal cross sections of the stack; higher (lower) resonance frequencies are expected for upper (lower) IJJs. This system has been discussed for more than 20 years [54] as a model of various synchronization phenomena found in nature and society [55]. The detailed mechanism of excitation of synchronised transverse

CONTENTS



Figure 2. Schematic illustrations of (a) transverse and (b) longitudinal Josephson plasma oscillations in stacked IJJs and (d) Josephson vortex lattice induced by an external in-plane field. In (c), a single Josephson junction is depicted with the definition of directions for comparison. Wavy surfaces in (a), (c), and (d) represent gauge-invariant phase difference between adjacent superconducting layers. In (b), a blue color tone of a superconducting layer represents the charge density due to Josephon tunnelling and green gradations illustrate induced electric potential.

Josephson plasma waves is thoroughly explained in previous review articles [53, 56] and more recent papers [57, 58, 59, 60, 61].

The Josephson plasma frequency ω_p can be measured using the Josephson plasma resonance in the long-wavelength limit by applying a uniform AC electric field along the *c*-axis over the *ab*-plane [16, 62]. For Bi2212, the Josephson plasma resonance was experimentally investigated in the micro- and millimetre-wave regions. At T = 0, $\omega_p/2\pi$ is in the range of 50-150 GHz depending on the anisotropy as shown in Table 4. The Josephson plasma resonance in Bi2212 under magnetic fields parallel to the *c*-axis has been employed as a sensitive probe of the coherence between the CuO₂ layers in vortex states [63]: ω_p shows abrupt changes accompanied by (possible) phase transitions of vortex matters [22, 23] and a higher order change in the correlations between pancake vortices defined within the CuO₂ layers [20, 21, 64] because fluctuating vortices reduce J_c with the increase in $\phi_{l,l+1}$ according to $J_c \propto$ $\langle \cos \phi_{l,l+1} \rangle$, where $\langle \cdots \rangle$ represents the thermal average [15, 17, 65, 66].

EM wave absorption of the transverse Josephson plasma depending on k_x , which is the opposite process against EM wave emission, has been investigated by varying either the planar sizes of Bi2212 single crystals or the periodicity of the JV lattice

(external field parallel to the *ab*-plane). The frequency of the transverse Josephson plasma increases with decreasing lateral sample size according to the strong dispersion relation of the transverse mode when an AC magnetic field is applied parallel to the *ab*-plane [62, 18]. The JV lattice induced by an external magnetic field parallel to the *ab*-plane, H_{ab} , modulates the Josephson plasma wave along both the *c*-axis and the *ab*-plane. In the high- H_{ab} region, where JVs penetrate all the block layers, the Josephson plasma frequency $\omega_p(H_{ab})$ increases linearly with H_{ab} . This is attributed to the increase in k_x yielded by the increase in H_{ab} under the intrinsic pinning [67, 68, 69]. Theoretically, numerical simulations of EM wave radiation by flowing JVs have been developed [70, 71, 72].

These experimental and theoretical evidences for coherent excitation of Josephson plasma waves inside IJJs have stimulated subsequent research for their emission. The rich variety of I - V characteristics of IJJs with lateral dimensions of a few μ m under magnetic fields parallel to the *ab*-plane have been found to reveal signs of the EM wave emission [25, 26, 73, 74]. The responses of detector Josephson junctions placed in the vicinity of oscillator stacks of IJJs have shown firmer evidence for excitation of EM wave from IJJs [75, 76]. The search for THz EM radiation is described in detail in Refs. [53] and [56].

The finding of Ozyuzer et al. [29] has three superiorities comparing with previous findings: (1) the large mesa with lateral dimensions of more than 50 μ m, which is formed by easily accessible fabrication techniques without the need for sophisticated methods; (2) explicit far-field detection with an ex-situ (outside the cryostat) detector through a few windows; and (3) the absence of an external magnetic field, which yields a simple and inexpensive experimental setup.

4. Experimental methods and emission properties

Since the first presentation of an IJJ THz source in 2007, extensive experimental and theoretical studies have been performed. Here, we describe the experimental procedure for obtaining an IJJ THz source and the features of IJJ THz source with emphases on emission conditions, emission intensity, and material evolution. Note that most of the features of the emission frequency and spectral linewidth revealed to date are covered by previous reviews [56, 77]. More recent progress involves expanding the highest emission frequency to 2.4 THz [34]. This topic is dealt with in the context of thermal management in Sec. 5.2.

4.1. Device preparation and measurement setups

Most of the IJJ THz devices are made of Bi2212 single crystals grown by the traveling solvent floating zone method. The mesa structures are shaped either by photolithography, metal-masked milling, or the focused ion beam (FIB) method. Among them, photolithography has been employed since this research began. The mesa and electrode patterns are designed in a photomask and are projected onto a thick (~ 10 μ m) photoresist layer coated on a Bi2212 crystal glued to a sapphire or MgO substrate. The crystal with the shaped photoresist is milled by an Ar ion shower machine. Figure 3(a) shows a schematic image of the mesa structure on a Bi2212 single crystal obtained by this method. Hereafter, we define x, y, and z axes as lying along the short edge in the ab-plane, the long edge in the ab-plane, and the c-axis stacking direction, respectively, as shown in Fig. 3. Typical dimensions are $L_x \times L_y \times L_z = (40-$



Figure 3. (a) Mesa and (b) stand-alone devices for the THz emitter. Coordinates and dimensions are also given. In the lower panels, red broken curves represent excited Josephson plasma waves and red solid arrows represent the surface current yielding the radiation of EM waves into space.

100) × $300 \times 1\mu$ m³. Since the photoresist pattern is remarkably reduced in both thickness and area, the mesa has a trapezoidal cross section in which the length of the top surface is approximately 10 % smaller than that of the bottom surface. This type of device has the disadvantages of poor heat transport and ambiguity of the number of working IJJs as discussed in Secs. 4.2 and 5. To avoid these problems, a stand-alone device was developed. In this device, the mesa is removed from the original Bi2212 base crystal and is glued to another substrate with higher thermal conductivity using a silver epoxy. For further heat elimination, sandwich structures have been reported very recently [32, 33]. Figure 4 shows the gold-Bi2212-gold (GBG) and sandwich structure (SWS), which were invented by one of the authors [32].

The metal-masked milling method employs a metal mask made by electroforming instead of using a photoresist like the photography method. This method makes it possible to have a thicker mesa because the metal mask is etched to a lesser degree by Ar ion milling than the photoresist. Because the FIB method does not require any mask, the mesa design is more flexible. In addition to the rectangular shape, circular [78], triangular [79], and pentagonal [80] shapes are formed by the FIB grooving on Bi2212 crystals. The required facilities and techniques for these and other methods are listed in Table 1. Chemical etching processes such as the hydrochloric acid modification method have the advantage of speedy fabrication of both in-line [81] and stand-alone [82] devices, although emission detection has not yet been successful.

9



Figure 4. Schematic views of (a) GBG and (b) SWS structures mounted on the silicon lens, which were developed for improving the heat elimination. (c) and (d) show close-ups of the IJJ stacks. (after [32])

Table 1. Device preparation methods. The standard of "Ease" is ... PL, PM, AL, Ar, EBL, and MM represent photolithography, photomask, alligner, Ar-ion milling machine, e-beam lithography, and metal mask, respectively.

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Method	Required techniques	Ref.
Photolithography	PM, AL, Ar	[29]
PL & Ti mask	PM, AL, Ar, EB-evapolator	[83]
e-Beam lithography	EBL,Ar	[84]
Focused ion beam	FIB	[78]
Metal mask	MM, Ar	[85]
Stand-alone	PL, FIB, MM	[86]
Double side	PL	[87]
Capped LPE	Step substrate, Furnace, PL	[88]
Substrate sandwich	MM, Substrate w. patterned electrodes	[32, 33]

The most sensitive emission detection method is lock-in detection with a Si bolometer cooled by liquid helium. An InSb hot electron bolometer, a pyroelectric detector, and a Golay cell can also be used for higher emission power. Table 2 lists the properties of the detectors. A low-pass filter (the typical cut-off frequency was 1 THz for most previous experiments) is inserted in front of the Winston cone to eliminate background thermal radiation. Figure 5 (a) shows a system typically used to detect EM wave emission and to determine the emission frequency. The stacked IJJs are cooled in a He-flow cryostat and are biased by either a function generator or a DC voltage (current) source. The temperature is monitored on the sample stage of the cryostat, which is regarded as a thermal bath. Since the source of the emitted EM wave is an oscillating current flowing along the short edge of the mesa, which is much shorter than the wavelength of the emitted EM wave in space, the emitted beam

Detector	Songitivity	Spood	Boguirod facilition	Pof
Detector	Sensitivity	speed	Required facilities	mer.
Si bolometer	Excellent	Fair	Liq. He	[29]
Pyroelectric sensor	Fair	Good	-	[89]
InSb hot-electron bolometer	Excellent	Good	Liq. He	[90]
Golay cell	Good	Poor	-	[91]
YBCO grain boundary junction	Good	Good	Inside cryo. w. emitter	[31]
Intrinsic Josephson junction	Good	Good	Inside cryo. w. emitter	[92]

 Table 2. Detectors suitable for IJJ THz sources.

diverges radially. An optical lens made of poly-crystalline Si or fused quartz placed above the mesa facilitates delivery of higher optical power to the detector.

Fourier transform infrared (FTIR) spectrometers are used to resolve the emission frequency. In addition to commercial Michelson and Martin-Puplett interferometers, as shown in Fig. 5 (b) laboratory-built interferometers are also used for spectroscopy. A simple lamellar interferometer [93] was introduced by Wang et al., as shown in Fig. 5 (c) [94]. This system does not require delicate alignment of the beam path, and most of the emitted optical power is delivered to the detector, whereas only 50 % of the optical power is delivered in a Michelson-based interferometer with perfect alignment. Note that lenses are inserted, as described in the previous paragraph, to make the alignment more accurate. Turkoglu et al employed a Si single crystalline wafer as the beam splitter of a Michelson interferometer [91]. The Martin-Puplett method is suitable for attaining higher frequency resolution by extending the traveling distance of one of the reflectors. Kakeya et al. built a spectrometer with a resolution of less than 1 GHz, which is one-order higher than that of an ordinary commercial spectrometer [95].

To determine the spectral linewidth with higher frequency resolution, a heterodyne mixing method is used. Kashiwagi et al. presented a power spectrum with $\Delta f \simeq 500$ MHz for emission at the centre frequency, $f_e = 638$ GHz, at $T_b = 10$ K [96]. Li et al. reported the sharpest linewidth of 23 MHz through measurements using a superconducting integrated receiver consisting of a superconducting flux-flow oscillator and a superconductor-insulator-superconductor harmonic mixer [97].

4.2. AC Josephson relation and cavity effect

In the first demonstration by Ozyuzer et al., THz emission was obtained in the retrap region, where the bias voltage V decreases rapidly with decreasing bias current I far below the maximum Josephson current. Subsequently, Kadowaki et al. found another type of emission that is more intense and stable at a higher current bias closer to (sometimes higher than) J_c [98]. A current–voltage (I - V) characteristic and EM wave detections as functions of I and V of a typical device [99] are plotted in Fig. 6 (a). We refer to the latter emission as "high-bias" to distinct it from the original emission found in the "low-bias" regime. The low-bias regime corresponds to I_1 in Fig. 6 (b) and the high-bias regime corresponds to I_2 and I_3 . Wang et al. also independently found THz emission from another IJJ device [94]. They reported for the first time that f_e in the high-bias regime depends strongly on bath temperature T_b and I. The relationship between f_e and V follows the AC Josephson relation given by Eq. (4).

The I - V characteristics of the outermost (McCumber) branch of the IJJ stacks



Figure 5. THz emission detection and spectroscopy setups. (a) An integrated system in which an emission power and an emission spectrum are simultaneously observed. (b, c) Martin-Puplet type and lamellar mirror type FTIR spectrometers. The frequency resolution can be improved by increasing the displacement between two mirrors. (after [98], [95], and [94], respectively)

found in the downward current sweep are remarkably nonlinear as illustrated in Fig. 6 (b) because of the following reasons. At bias currents sufficiently higher than the critical current (above I_3), the device temperature may be more than 10 Kelvins higher than T_b because of self-heating of the device and poor thermal conductivity of Bi2212. Since the c-axis resistivity of Bi2212 IJJs in the normal state is expected to maintain the rapid increase with decreasing temperature even below T_c , the decrease in the device temperature due to the decrease in I causes an increase in P below I_2 . A further decrease in I restores the zero-resistance of IJJs. Note that the c-axis bias current accumulates at which the local temperature is higher (local resistance is lower) and this accumulation makes the non-linearity of the I - V characteristics more significant. The local temperature rise above T_c is referred as a "hotspot" and is discussed in Sec. 5.1. The resultant S-shaped I - V curve as shown in Fig. 6 (b), provides up to three bias currents I_1 , I_2 , and I_3 with the same V, which induces an EM wave with $f = 2eV_b/Nh$ according to the AC Josephson relation (Eq. (4)), where N is the number of IJJs in voltage state. The emission occurs when f_e matches to a cavity resonance condition as described in the following paragraphs.

The emission phenomena in the low-bias regime (I_1) are less controversial than those in the high-bias regime $(I_2 \text{ and } I_3)$. The emission frequency is primarily explained by a matching effect between the AC Josephson effect and the cavity resonance of the TM(1,0) mode in the mesa structure [29]. The emission is less stable because some of the stacked IJJs return to zero-resistance (retrapping) in this current region, resulting in a sudden voltage drop with decreasing current. On the other hand, the high-bias regime exhibits a rich variety of phenomena such as broad-band frequency tuning, significant local temperature increases, and surprisingly narrow spectra [98, 100, 94, 97]. The directionality and duration of continuous emission were initially tested for high-bias emission, providing relevant intuition for excitation inside the mesa [89]. A few reports mention emission at the highest bias currents corresponding to I_3 [101, 102]. The emission frequency in this regime is significantly lower than that predicted by the AC Josephson relation [102]. This is explained by a significant temperature gradient along the stack (c-axis): uniformly hotter layers near the surface determine the emission frequency, whereas colder layers near the bottom contribute to the excess voltage.

The cavity model gives the frequency of the excited transverse Josephson plasma wave inside a rectangular IJJ stack shown in Fig. 3 (a) as follows:

$$f_{m,p}^{c} = \frac{c_0}{2n} \sqrt{\left(\frac{m}{L_x}\right)^2 + \left(\frac{p}{L_y}\right)^2},\tag{5}$$

where n is the refractive index of the mesa, and m and p represent the number of nodes of the standing wave along the x and y directions, respectively. In a mesa with a large aspect ratio $(L_x \ll L_y)$, since the emission frequency is proportional to $1/L_x$, primarily the TM(1,0) mode is excited. The details are described in Sec. 5.1. In a mesa with an aspect ratio close to unity, we often observe emissions attributed to various cavity modes TM(m, p). The agreement with experimentally observed emission frequencies is summarised in Fig. 7. However, it is still difficult to unambiguously determine the cavity mode because the emission intensity is rather continuous with respect to the frequency owing to the degeneracy in frequencies of different modes [86]. Even mesas with circular [78], triangular, and pentagonal [79] shapes emit not only with certain cavity modes but also with undefined modes. Quite recently, excellent



Figure 6. (a) I - V characteristics (main) and bolometer response (bottom and right) for an IJJ THz sources at $T_b = 50$ K. Arrows indicate scanning directions. With increasing I, V jumps from 0.17 to 0.77 V at the critical current approximately 25 mA. Then the device starts to emit EM wave. With decreasing I from its maximum, V traces a different path below the critical current. EM wave emissions are observed at high-bias region (18 < I < 30 mA) and low-bias region (6 < I < 10 mA). Discontinuities of the I - V curve below 10 mA starting at the low-bias region are due to the retrapping (see text). (b) Schematic illustration of the S-shape behaviour in an I-V curve of the outermost branch. With decreasing bias current, the device temperature decreases, and then the superconducting gap Δ increases. In the higher current limit (normal state), the I-V curve should asymptote to the Ohmic line indicated by a broken line.

correspondence between emission peaks and cavity modes was reported throughout numerical calculations [103].

For tuning emission frequency f_e of one device in-situ, either n, L_x , or L_y has to be modified effectively by tuning bias conditions and T_b . The wide-range tuning of f_e of the IJJ THz source arises effective variations in n, L_x , and L_y due to change of device temperature. The effective n depends on device temperature through the temperature dependence of the London penetration depth λ_L in the presence of the longitudinal component of an excited Josephson plasma oscillation (finite k_z) [104]. With increasing device temperature, f_e decreases through the decrease in propagating speed of the Josephson plasma oscillation due to the increase in λ_L . The increase of I raises device temperature, also resulting in the decrease of f_e [105]. The effective changes of L_x and L_y are discussed in Sec. 5.1.

The emission power P was found to be much more intense in the z-direction than in the x-direction [98], although the first observation was monitored only in the xy-direction [29]. This result suggests that the alternating current induced by the transverse Josephson plasma oscillation appears not only on the yz-surface but also on the xy-surface of the mesa. The alternating current is inductively coupled with the space, resulting in a propagating EM wave polarised along the x axis. For the TM(1,0) mode, the emission intensity is greatest in the direction tilted by 20-30 ° from the z-axis toward the xy-plane, according to directionality measurements in the



Figure 7. Plot of the typical emission frequencies vs several cavity resonance modes. c_0 is the speed of light in vacuum, and n is the refractive index of the material. w and L correspond to L_x and L_y in the present review, respectively. (after [96])

xz-plane. [89] This is attributed to interference between a wave coming directly from the mesa and a wave reflected by the superconducting substrate. For an asymmetric device in which a mesa is placed at an apparently off-centred position on the substrate, the directionality becomes asymmetric [106].

4.3. Emission intensity

The emission intensity is one of the most important parameters describing the performance of an EM wave source. To date, a maximum total emission power of $P_{tot} = 610 \mu W$ has been achieved by synchronising three IJJ stacks at $T_b = 40$ K [106]. Note that direct comparison of the emission (detection) power among groups and comparison with other THz sources are difficult because the total emission power P_{tot} is estimated assuming losses in the optical components, and the detected power P sometimes represents the beam power focused by a lens. Table 3 summarises the

powermeter, and grain-boundary junction, respectively.						
Device type	reported power	Detector	Estimation	Note	Ref.	
Single mesa	$30 \ \mu W$	Si-BM, InSb-BM, PM	directionality in two planes	Integ. pow.	[107]	
Sync. 3 mesas	$610 \ \mu W$	Si-BM	calib. by a black-body source	Integ. pow.	[106]	
Single mesa	$110 \ \mu W$				[106]	
Double-sided	$82 \ \mu W$	Si-BM, YBCO GBJ		Direct detection	[32]	

Table 3. Summary for emission powers. BM, PM, and GBJ represent bolometer, powermeter, and grain-boundary junction, respectively.

maximum emission powers reported by various groups [31, 106, 107].

The first reliable estimation of P_{tot} considering the directionality was 5 μ W [89], and a higher P_{tot} of 30 μ W was subsequently reported by Yamaki et al. [108] More exact estimations were recently presented by Sekimoto et al. [107]. They reported a $P_{tot} = 30\mu$ W after careful calibration of their detection setup and emission directionality as shown in Fig. 8. An InSb hot electron bolometer calibrated by a blackbody radiation source was used for detection, in addition to a Si bolometer and a commercial power meter. The results obtained from the three different detectors show good consistency.

To increase the emission power, synchronisation of multiple mesas has been attempted since the early research. The pioneering result was obtained by Orita et al. [85] Two mesas with slightly different emission frequencies (0.68 and 0.70 THz) were electrically connected in series and driven simultaneously. As a result, the two mesas emitted EM waves at another frequency (0.65 THz), and the maximum P significantly exceeded the sum of the individual emissions. Benseman et al. were able to detect the maximum power emitted from an IJJ device, which is $P_{tot} = 610\mu$ W at 510 GHz by synchronising three mesas on a Bi2212 single crystal biased in parallel as shown in Fig. 9 [106]. They carefully calibrated their detection system with a standard black-body radiator and managed the huge amount of dissipated from a crystal soldered onto a metallic copper substrate. The emitted EM waves were monochromatic up to the resolution limits of their spectrometers; thus, the EM waves excited in the individual mesas are synchronised.

The stand-alone devices illustrated in Fig. 3(b) were originally invented to increase the emission power. These attempts were based on a theoretical suggestion that the image super-current flowing in the superconducting substrate underneath the mesa diminishes the emission power [109]. Although the early preparation procedures for the stand-alone devices were technically complicated [96, 110, 105], Kashiwagi et al., developed an easier procedure to obtain systematic results [111]. The emission power from stand-alone devices tends to be higher than that from conventional mesa devices [110]. However, the direct contact of the mesa with the substrate facilitates thermal dissipation into the substrate rather than removal of the image current. An et al.[31] combined a stand-alone Bi₂Sr₂CaCu₂O₈ IJJ stack, emitting THz radiation, with a YBa₂Cu₃O₇ grain boundary Josephson junction acting as a detector. With the emitter radiating at 0.5 THz, they observed up to seven Shapiro steps in the I - V characteristics of the detector. The AC current induced in this detector junction was $I_{ac} = 0.93$ mA, which indicates that the power picked up by the antenna is $P = I_{ac}^2 Z/2 \approx 82 \,\mu$ W, where the impedance of the antenna $Z \approx 189 \,\Omega$.



Figure 8. (a) The definitions of θ_1 and θ_2 . (b) Polar plots of the radiation intensity $I(\theta_1)$ normalized at I(0) measured in the *xz*-plane at 55 K. (c) Polar plots of $I(\theta_2)$ normalized at I(0) measured in the *yz*-plane at 55 K. (after [107])

4.4. Suitable materials

It is well-known that the T_c value of high- T_c cuprates depends strongly on the carrier doping p, where T_c exhibits a dome-shape as a function of p [112]. The carrier doping also changes the IJJ properties; with decreasing p, J_c decreases exponentially, the quasiparticle tunnelling resistivity increases, and phase diffusion is less pronounced. Because the THz emission from IJJs was first demonstrated in strongly under-doped Bi2212 with $T_c \simeq 70$ K, an under-doped crystal is believed to be more suitable for THz emission. Certainly, a higher V due to the higher quasiparticle resistivity gives rise to a higher f_e satisfying the Josephson relation [Eq. (4)]. Moreover, the lower retrapping current when the IJJ returns to the superconducting state, which occurs because there is less phase diffusion (damping), expands the voltage region in which the emission condition is satisfied, especially for low-bias emission. Nevertheless, it has been found that under-doping is not essential for emission. Intensive emission is reported in crystals with higher J_c values and $T_c \simeq 90$ K. Figure 10 plots f_e versus the critical current density J_c , where the symbol size and colours represent L_x and the measured T_b , respectively. f_e is obtained from the spectrum with the maximum peak height among spectra taken under various bias voltages and temperatures for a



Figure 9. (a) Bias dependence of the THz emission power P_{tot} of an array of mesas for various activated mesas and the maximum power as a function of the number of activated mesas and (b) emission spectrum of the array for various activated mesa. (after [106])



Figure 10. Emission frequencies as a function of J_c . Symbol sizes and colours represent L_x and measured temperatures. A solid line represents $f_e \propto \sqrt{J_c}$. Data correspondences are A07 [29], A11 [104], I12 [91], I13 [113], K15-1 [105], K15-2 [114], N10 [94], N12 [87], N14 [32], T09 [89], T12-1 [96], T12-2 [86], T14 [110], T15-1 [33], and T15-2 [34].

specific device. The upper limit of the optimised frequency appears to depend on J_c rather than L_x and roughly follows $\sqrt{J_c}$, which is the same evolution as the Josephson plasma frequency ω_p .

Very recently, emission from Bi2212 substituted materials has been reported. Tsujimoto et al found emission from Pb-Bi2212 stacks with a J_c value three times larger than that of usual pristine Bi2212 mesas [114]. To suppress the temperature rise, a stand-alone device was used. The emission frequency was found to be almost twice that expected in a pristine Bi2212 device with the same dimensions. The effective refractive index is presumably smaller in Pb-Bi2212. More recently, emission was also found in La-Bi2212 which is expected to have less damped IJJs. Material evolution has great potential for the functionalisation of IJJ THz sources because the junction parameters can be tuned over a wide range. Related parameters of IJJ materials are listed in Table 4

5. Thermal management of IJJ THz sources

In most experiments to date, the emission frequencies were well below the frequency corresponding to the superconducting gap energy of Bi2212. The main obstacle to emission at higher frequencies is self-heating, which limits the maximum voltage V_{max} across the stack. Self-heating is more severe when there are more junctions

of IJJ materials. " $\rightarrow 0$ " represents extrapolation to 0 K.					
Material	T_c [K]	ϵ	$\omega_p/2\pi \; [\text{GHz}]$	T [K]	Ref.
Bi2212	70.2		56.8	$\rightarrow 0$	T-scan at various ω [69]
Bi2212	68.0		68	$\rightarrow 0$	ω -scan [19]
Bi2212	82.5		124	$\rightarrow 0$	ω -scan [19]
Bi2212	90	12		6	FTIR [115]
Bi2212	85		150	5	FTIR [116]
Bi2212	71		330	5	FTIR [116]
$Bi_{1.6}Pb_{0.6}Sr_{1.8}CaCu_2O_{8+\delta}$	65	11.5	1150	8	FTIR [117]
La-Bi2212 $(p = 0.168)$	85	6	186	20	19 GHz, 30 kOe [118]
Bi2201	16.5		67	$\rightarrow 0$	ω -scan [19]
$Nd_{1.85}Ce_{0.15}CuO_4$	18.0	14	174	11	T-scan at fixed ω [119]
$Tl_2Ba_2Ca_2Cu_2O_8$	103.4	9.1	780	10	THz-TDS [120]

Table 4. Reported dielectric constants ϵ and Josephson plasma frequencies $\omega_p/2\pi$ of IJJ materials. " \rightarrow 0" represents extrapolation to 0 K.

in the stack and in stacks with larger lateral sizes. As a result, we typically observe severe bending of the I - V curves at high bias currents or voltages. The strong temperature inhomogeneity has been studied experimentally and theoretically [100, 102, 121, 122, 123, 124, 125]

5.1. Temperature inhomogeneity

The first representation of temperature inhomogeneity was reported using the LTSLM [100]. The principle of the LTSLM is described in the supplementary material of Ref. [100]. In short, the beam of a diode laser with a spot size of $1 - 2 \ \mu m$ is deflected by a scanning unit and focused onto the sample surface. Local heating by 2 - 3 K in an area of a few μm^2 and about 0.5 μm in depth causes a change in the voltage across the mesa, ΔV , which is detected using lock-in techniques, and serves as the contrast of the LTSLM image. Standing waves can also be imaged by using a local change in the quality factor induced by the laser beam. This results in a stronger ΔV signal at antinodes and a weaker signal at nodes.

Recently, a mini-LTSLM was developed on the centimetre scale [126]. A schematic of the mini-LTSLM is shown in Fig. 11. A sample is mounted on a hemispheric sapphire lens. A laser with wavelength $\lambda = 1310$ nm and a spot diameter of about $1 \,\mu$ m is focused onto the surface of the stack. The laser can scan across the surface of the stack with submicron precision. Thanks to the small size of the setup which includes a Si bolometer, it can also measure the emission power of the sample from the other side of the hemispheric lens while the laser is kept on at the same time [126]. The power detection and frequency measurement are similar to the previous work [127]. By modulating the laser power using a 10 kHz square signal, we detect the global differential voltage response ΔV of the stack with a lock-in technique while the sample is biased at a constant current. In this case, the setup serves as an LTSLM [100, 94, 127, 128]. Recently, Zhou et al. used a relatively strong beam power to operate the LTSLM in a manipulation mode at the same time.

Joule heating in large Bi2212 mesas was numerically analysed by considering the typical terminal conductivity and the temperature dependence of all the materials associated with heat dissipation and removal. Such mesas are used in experiments on THz-range radiation. The analysis shows that the temperature increases with



Figure 11. Sketch of mini-LTSLM system for the GBG structure sample on a hemispheric sapphire lens. A focused laser can scan across the sample surface while emission is detected through the lens by a Si bolometer (not shown in the sketch). This system allows us to measure simultaneously both changes in voltage of the device and emission power due to the focused laser irradiation. (after [126])



Figure 12. Power density dissipated by in-plane currents for five values of normalized bias current at upper left and maximum dissipation current at bottom left. The grey square in (a) indicates position of the bond wire. Black curves are drawn where the local temperature corresponds to T_c and the regions closer to the injection point are at temperature higher than T_c . (after [125])

increasing I and is distributed unevenly along the mesas. The temperature of the mesa's central part can even exceed T_c at sufficiently high bias, forming a hotspot. The overall I - V characteristics are also calculated self-consistently and show a negative differential conductance for a wide range of currents [121]. Gross et al. reported similar results on hotspot formation in stacks of IJJs in Bi2212 [128]. The formation of hotspots in this system is shown to arise mainly from the strongly negative temperature coefficient of the *c*-axis resistivity of Bi2212 at low temperatures.

Quite recently, Rudau et al. used 2D coupled sine-Gordon equations combined with three-dimensional heat diffusion equations to numerically investigate the thermal and EM properties of a 700-IJJ stack [125]. Typical numerical simulation results are shown in Fig. 12. A strong field -induced enhancement of P by a factor of almost 3 was found experimentally, for an applied field of around 5.9 mT. Although the numerical simulations are in good agreement with the experimental observations, direct measurement of the temperature is required to confirm these experimental and theoretical results.

Two fluorescence methods have been employed to monitor local variation in the mesa temperature: coating the device with a polymer film containing the rareearth Eu [102, 123, 129]or spreading SiC nano-crystals [122] over the device. The strong temperature dependence of the fluorescence intensities excited by ultraviolet irradiation is used to display the temperature distribution at the device surface. The distribution of the fluorescence intensity is magnified by a microscope and monitored by either a (Peltier-cooled) CCD or CMOS camera. The observed fluorescence intensities under a bias are converted into local temperatures using calibration data obtained at a uniform temperature without an electrical bias on the device.

The temperature image of a mesa surface reveals a highly inhomogeneous temperature distribution with a hotspot around the centre of the mesa. Benseman et al revealed that a faint hotspot with a maximum local temperature of $\sim T_c$ appears at the centre of the mesa in the low-bias emission regime, and a more significant and oscillatory temperature rise is observed at currents much higher than those of the high bias regime. [102]. The results are consistent with solutions of the heat diffusion equation in the model connecting with the thermal bath only through the superconducting substrate [121]. Minami et al. concluded that the temperature inhomogeneity has nothing to do with the emission, although a hotspot is observed in the high-bias regime [122]. Tsujimoto et al. found that the emission intensity is higher for a nonuniform bias configuration with a weaker hotspot as indicated by the blue plot in Fig. 13 (b), and thus the volume fraction of the superconducting component contributes to the emission power P [123]. The difference in the temperature distribution was explained by considering thermal escape through the electrode. For the nonuniform bias, heat elimination through the electrodes is more efficient to decrease the extent of the hotspot than that for the uniform bias, because the hotspot center locates underneath the biasing electrode, which also works for a heat path, for the nonuniform bias, whereas in-between the two electrodes for the uniform bias.

5.2. Heat manipulation

To actively manipulate the self heating in the mesa, a novel structure was invented by sandwiching the stack between a pair of substrates. As a result, THz emission above 77 K (liquid nitrogen temperature) was realised, and the frequencies were increased to



Figure 13. (a) I - V characteristics of a device for nonuniform (bias current is injected through one electrode) and uniform bias (bias current is injected through two electrodes) at $T_b = 20$ K. Bolometer responses P as functions of bias voltage V in the high- and the low-bias regime are shown in (b) and (c), respectively, where the blue and the red plots indicate the data for nonuniform and uniform bias. V for the latter case has offsets of 0.2 V. The insets above the data present the corresponding temperature distributions in the mesa. (after [123])

1.05 THz as shown in Fig. 14 [32]. In subsequent experiments, the frequencies were increased to 1.6 and 2.4 THz with a similar sample configuration[33, 34].

Wang et al. started by fabrication of a Bi2212 stack embedded between two gold layers using a previously reported process [130]. The GBG structure sample emits in the range of 0.43 - 0.82 THz. They then glued a second, thermally anchored substrate onto the sample surface (SWS structure). The maximum voltage of this better cooled and dimensionally-unchanged sample increased [32]. Thus, both the emission frequencies and tunable frequency range were significantly increased to 1.05 THz and 0.71 THz, respectively. Sketches of the GBG structure are shown in Fig. 4(a) and (c) and sketches of the SWS structure are shown in Fig. 4(b) and (d). The fabrication details are described in Ref. [32].

The frequency ranges of detectable emission of both the GBG structure and the SWS with respect to T_b and V are summarised in Fig. 14(a). Both structures exhibit the same tendency, namely, the emission frequencies gradually increase with decreasing T_b . The GBG structure was found to radiate emission at several values of T_b s below 65 K, whereas the emission from the SWS can be detected over a broader temperature



Figure 14. Emission frequency f_e vs. (a) the T_b . (b) shows the spectrum of THz emission at $T_b = 20$ K and I = 3.037 mA. (after [32]).

range from 20 to 80 K, indicating that the operating temperature can be in the liquid nitrogen temperature range. For the entire temperature regime the SWS exhibited an emission frequency range (0.34 - 1.05 THz) that is much broader than that of the GBG structure (0.43 - 0.82 THz). Note that for the SWS emission above 50 K was observed in the low-bias regime. In addition, the highest f_e of 1.05 THz, for which the corresponding spectrum is shown in Fig. 14(b), was observed in the low-bias regime of the SWS. Figure 15 shows the typical spectra emission at 1.6 and 2.4 THz, as reported in Refs. [33] and [34]. Their expansions of the upper limit of emission frequency were achieved by attaching sapphire substrates both sides of mesas without superconducting substrates (stand-alone samples) [111].

Kakeya et al. argued that an electrode 400 nm in thickness suppresses the emission because the temperature distribution is too homogenised to induce the synchronization of spatial phase difference [99]. The electrode shape (impedance) is also relevant to the emission properties because a stripline that consists of two electrodes and a mesa possibly carries the excited high-frequency power to the ground. The strong frequency dependence of P is presumably related to the frequency dependence of the transmission loss of the stripline. Electrodes designed for optimising both the heat escape and emission efficiency are the next concern for IJJ THz sources.

A practical method of realising intense THz emission from IJJs using external local-heating was proposed and demonstrated theoretically [58]. An artificial temperature distribution induced by local heating strongly excites Josephson plasma waves inside IJJs. Accordingly, P_{tot} of the THz waves is enhanced dramatically, and can reach on the order of milliwats. Zhou et al. [126] reportedly tuned the THz emission of a Bi2212 IJJ stack by a focused laser beam that was scanned across the stack. The emission power P increased by up to 75 % upon laser irradiation at a T_b near 22 K. The laser-induced changes in the voltage V across the stack and in P were measured simultaneously. The maximum laser-induced change in the emission power ΔP , was achieved by irradiation from a position where the local temperature is approximately equal to the critical temperature T_c . However, ΔP was found to be proportional to the laser-induced global voltage change ΔV irrespective of the laser position. This unexpected *global* response is likely to be related to a change in the average stack temperature and is consistent with the change in P when T_b is increases by about 0.2 K. This tuning method can be employed in the application of Bi2212



Figure 15. Spectra of THz emission from (a,b) a rectangular mesa emitting up to 1.6 THz, and (c) a disk mesa emitting up to 2.4 THz. Both are stand-alone samples sandwitched by sapphire substrates. (after [33] and [34])

THz sources. Watanabe et al. [131] also observed that when the hotspot position was moved to a mesa end by locally heating the mesa surface with a laser beam, the intensity of the emission increased, but no changes in its frequency or line width were observed. These results suggest that higher power radiation is attainable by adjusting the hotspot position. Note that the beam size here is about 80 μ m in diameter; this is much larger than $1 - 2 \mu$ m, which was the typical value in Zhou et al.'s experiment.

6. Examples of applications of terahertz EM wave sources

This section describes practical applications of IJJ THz sources. To date, IJJ THz sources have been tested for nondestructive imaging. THz emission above 77K allows the use of compact configurations of an IJJ THz source cooled by liquid nitrogen.

THz waves can be transmitted through paper objects because of their submillimetre wavelength. One applications of THz waves is the inspectin of the contents inside packages and personal belongings hidden inside clothing. Tsujimoto et al. demonstrated that an IJJ THz source, like other THz sources, can be used for transmission imaging [90]. They provided transmission images of coins inside an envelope and a dandelion leaf. Interference fringes shown in the transmission image also illustrate the monochromaticity of the emitted THz waves. Kashiwagi et al.

have presented a reflection image of coins and a computed tomographic image of a three-dimensional object [132, 133].

Portability is one of the most important properties affecting practicality. The recent demonstrations of IJJ THz source above 77 K [134, 135] allow us to realise a compact THz source consisting of a battery and liquid nitrogen. The recent development of a Stirling cryocooler [136], which is compact and requires no external compressor, enables an all-in-one portable system of high- T_c devices operated above 40 K. The IJJ THz source is one of the best applications of the Stirling cryocooler because the performance of the IJJ THz source is optimised in the temperature range between 40 and 60 K. Reductions in the price of the Stirling cryocooler are quite an important factor for broad adoption of IJJ THz sources.

The emitted THz waves are expected to be coherent because the emission is driven by the synchronization of the stacked IJJs. The coherence, nevertheless, has to be demonstrated in an more explicit manner. High coherence is a least requirement for use of the IJJ THz source as a source of carrier wave for high-speed data transfers such as uncompressed high-resolution (for example, 4K resolution) movie files. To this end, we should be able to modulate the emitted THz waves. The use for local oscillators of superconducting mixers employed for astronomical observations [137] is one of the best promising applications because another cooling system is not required. For mobile communications, the generation of circularly polarised waves is important. Because an IJJ stack functions as a patch antenna, circularly polarised emission can be obtained by changing the mesa shape [138]. This is also an advantage of our IJJ THz sources. Finally, the circularly polarised THz waves can also be used in circular dichroism spectroscopy to identify harmful chemicals.

7. Summary

The properties of IJJ THz sources are described in this review. These sources possess an extremely broad frequency tuning range of more than 30 % of the central frequency. This remarkable advantage is considered to be attributed to the effective changes in propagation velocity of the excited Josephson plasma oscillation and geometries of the device, both of which are caused by peculiar properties of superconductivity such as strong temperature dependence of the penetration depth and the low thermal conductivity. A large part of the emission frequency range covers a temperature region of $k_B T > h f_e$, where CW-QCLs are disable to work, with a higher emission power than RTD oscillators. In addition to this, expected high coherence of emitted EM waves is also attributed to superconductivity as a macroscopic quantum phenomenon in solids. The ease of device preparation from a Bi2212 single crystal provides great potential for expanding research opportunities and promoting the use of the device for general purposes such as high-speed telecommunications and nondestructive spectroscopy. Thermal management is found to be an important factor for increasing the emission power and frequency of IJJ THz sources. Another important element is the electrode, which also works as an antenna. The performance of IJJ THz sources must be improved greatly by optimising the thermal management and impedance matching with the space.

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